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# Simulation of Rapid Thermal Annealing of Low-Energy Implanted Arsenic in Silicon

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Two-dimensional model of As thermal diffusion is presented. The model was developed taking into consideration nonlinearity of the process, cluster formation, influence of point defects. For the calculation of the impurity distribution profile at rapid thermal annealing, an efficient numerical algorithm based on a finite-difference method was applied. Results of calculations are compared to experimental data.

Key words: Numerical simulation, diffusion and ion implantation technology, defects, impurities, silicon

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#### Introduction

Low-energy ion implantation is widely used for the formation of active areas in modern integrated microcircuits elements. The combination of low-energy (1-30 keV) ion implantation and rapid thermal annealing allows fabricating devices with ultra-shallow junctions [1–4]. Such technologies of impurity doping lead to the formation of impurity profiles of a complex shape [5, 6]. The modelling of such processes is impossible without application of physical and mathematical description with a high degree of adequacy as well as involving effective numerical methods. Application of the commonly used process simulators like ATHENA SSUPREM4 of SILVACO not always provides satisfactory accurate results. In a surface region of the semiconductor (1–50 nm depth), the impurity distribution profiles calculated using such software can essentially differ from experimental results [5, 6]. At the same time, the exact information on dopant distribution in proximity of the surface is necessary for effective calculation of the electric characteristics of modern semiconductor devices.

In the present work, the two-dimensional model of thermal diffusion of arsenic in silicon is developed on the basis of our researches [7–9]. In our model, the migration of implanted arsenic is described in view of nonlinearity of the process, influence of point defects, cluster formation and migration of electrons. In contrast to the known models of arsenic diffusion in silicon, we consider that clusterization depends not only on a level of

the impurity concentration, but also on concentration of electrons. Such approach allows to model precisely enough distribution of the impurity at a surface of semiconductor crystal at low-energy implantation and rapid thermal annealing.

For the numerical solution of the constructed nonlinear systems of differential equations, the method of final differences [10, 11] is used. We developed the economic locally-one-dimensional schemes [11] allowing to model the diffusion in two dimensions quickly enough. Results of some numerical calculations, in comparison with experimental data, are presented.

# I. The model

We suggest that arsenic diffusion occurs due to the formation, migration, and dissociation of the "As<sup>+</sup>D<sup>r</sup>" pairs, where As<sup>+</sup> and D<sup>r</sup> are the substitutionally dissolved arsenic atom and intrinsic point defect, respectively [12]. At a construction of the model of point defects evolution we do certain simplifications. We assume that As diffusion occurs substantially by the interstitial mechanism, and diffusion by vacancies is less significant. Therefore we consider only the equation describing diffusion of point defects induced by transfer of intrinsic interstitial atoms. We assume also that the drift of internal elastic stress is negligible. A thermodynamic approach based on the local equilibrium

between the substitutionally dissolved arsenic, point defects and the pairs leads to the following system of diffusion equations:

$$\frac{\partial C^{\mathrm{T}}}{\partial t} = \sum_{k=1}^{2} \frac{\partial}{\partial x_{k}} \left( D(\chi) \left( \frac{\partial}{\partial x_{k}} (\tilde{C}C) + \frac{\tilde{C}C}{\chi} \frac{\partial \chi}{\partial x_{k}} \right) \right), \quad (1)$$

$$\sum_{k=i}^{2} \frac{\partial^2 \tilde{C}}{\partial x_k^2} - \frac{\tilde{C}}{l_i^{\times 2}} + \frac{\tilde{C}^g}{l_i^{\times 2}} = 0, \qquad (2)$$

where (1) is the equation of dopant atoms diffusion and (2) is the equation of diffusion of point defects [9];

$$C^{T} = C + C^{AC}, \qquad C = C^{*}/C_{i}^{*}, \qquad D_{i} = D_{i}^{*} + D_{i}^{i} + D_{i}^{2},$$
$$D^{C}(\chi) = \frac{1 + \beta_{1}\chi + \beta_{2}\chi^{2}}{1 + \beta_{1} + \beta_{2}}, \quad \beta_{j} = \frac{D_{i}^{j}}{D_{i}^{*}}, \quad j = 1, 2,$$

where C and  $C^{4C}$  are the concentrations of substitutionally dissolved arsenic atoms and dopant atoms incorporated into clusters, respectively;  $D = D(\chi)$ and  $D_i$  are the effective and intrinsic diffusivities of arsenic, respectively;  $D_i^{\times} D_i^1$ , and  $D_i^2$  are the partial diffusion coefficients due to interactions of the dopant atoms with the neutral, singly, and doubly charged defects, respectively;  $\chi$  is the concentration of electrons normalized to the intrinsic carrier concentration  $n_e$ ; C<sup>×</sup> is the concentration of point defects in the neutral charge state;  $C_i^{x}$  is the equilibrium concentration of neutral point defects in the bulk of the semiconductor,  $l_i^{\times}$  is the average migration length of point defects;  $\tilde{C}^{g}$  is the effective generation rate of point defects normalized to the rate of equilibrium thermal generation:

$$C^{g} = 1 + g(x_{1}, x_{2}) / g_{i},$$

where  $g_i$  is the total defect generation rate in different charge states in an intrinsic semiconductor; the function  $g(x_1, x_2)$  in the case of  $l_i^{\times} \ge \Delta y^d$  and  $l_i^{\times} \ge \Delta R_p^d$  can be approached by the following analytical expression [13]:

 $g(x_1, x_2) = \frac{G(x_1)}{2} \left[ \operatorname{erf}\left(\frac{x_2 + a}{\sqrt{2}\Delta y^d}\right) - \operatorname{erf}\left(\frac{x_2 - a}{\sqrt{2}\Delta y^d}\right) \right].$ Here

$$G(\mathbf{x}_{1}) = \frac{p^{d}}{\sqrt{2\pi}\Delta R_{p}^{d}} \exp\left[\frac{(\mathbf{x}_{1} - R_{p}^{d})^{2}}{2(\Delta R_{p}^{d})^{2}}\right],$$

where  $p^{d}$  is the defect generation power at arsenic ion implantation,  $R_{p}^{d}$  is the position of maximum of generated defects distribution,  $\Delta R_{p}^{d}$  is the depth dispersion,  $\Delta y^{d}$  is the lateral deviation of the generated defects. The concentration of clustered arsenic atoms can be obtained from the following expression [9]:

$$\mathbf{C}^{\mathrm{AC}} = \mathbf{K} \tilde{\mathbf{C}}_{\mathrm{D}} \chi^4 \mathbf{C}^2 ,$$

where *K* is the characteristic parameter of clustering;  $\tilde{C}_D$  is the normalized concentration of the defects participating in the cluster formation. We used the  $K\tilde{C}_D$  value of  $3.0 \times 10^{-16} \,\mu\text{m}^3$  at a temperature of 950 °C. The parameter value has been taken from [9]. To calculate values of  $\chi$ , a condition of local charge neutrality was used:

$$\chi = n/n_{e} = \frac{C - C^{AC} - C^{B} + \sqrt{(C - C^{AC} - C^{B})^{2} + 4n_{e}^{2}}}{2n_{e}}, (3)$$

where  $C^{B}$  is the summarized concentration of acceptors.

The simulation domain is considered as a flat cut of a masked silicon substrate transversely to the surface (Fig. 1):  $G = \{0 \le x_1 \le l_1, 0 \le x_2 \le l_2\}$  is a rectangle with sides  $l_1$  and  $l_2$ , A is the border of simulation area:  $A = A_1 + A_2 + A_3 + A_4$ , 2a is the width of not-masked surface.



**Fig. 1.** The simulation domain and the normalised twodimensional distribution of point defects.

For the Equation (1) on the boundary A let us consider the following condition:

$$D(\chi) \left( \frac{\partial \tilde{C}C}{\partial n} + \frac{\tilde{C}C}{\chi} \frac{\partial \chi}{\partial n} \right) = 0, \qquad (4)$$

where **n** is the normal vector to the simulation boundary. The initial conditions are following

$$C^{T}(x_{1}, x_{2}, t)\Big|_{t=0} = C_{0}(x_{1}, x_{2}),$$
 (5)

where  $C_0(x_1, x_2)$  is the distribution of the implanted atoms.

Equation (2) is closed by the conditions:

$$\tilde{C}\Big|_{A_1} = \alpha(x_2),$$
where  $\alpha(x_2) = \begin{cases} \alpha - \text{const} < 1, & \text{if } 0 \le x_2 \le a, \\ \beta, & \text{if } a < x_2 \le l_2 \end{cases}$ 

$$\tilde{C}\Big|_{A_2} = 1, \tilde{C}\Big|_{A_3} = 1, \frac{\partial \tilde{C}}{\partial x_2}\Big|_{A_4} = 0.$$
(6)

In case of a mask, for example, from silicon nitride,  $\beta = 0$ .

#### **II.** Numerical method

For the purpose of calculation acceleration, it is possible to use domains of different size for As atoms and point defects diffusion modelling. The values of  $l_1$  and  $l_2$  for the solution of Eq. (2) should be large enough to guarantee correctness of the boundary conditions  $\tilde{C}|_{A_2} = 1$  and  $\tilde{C}|_{A_3} = 1$ . At the same time, the

problem of the modelling of low-energy implanted dopant is solved, as a rule, in much smaller area. Therefore, it is enough to take the defects distribution corresponding to the area of modelling of As diffusion (Eq.(1)) with the purpose of reduction of the calculation time.

Let us introduce a non-uniform time grid:

$$\omega_{\tau} = \left\{ t_0 = 0, \, t_j = \sum_{k=1}^{J} \tau_k \,, \, j = 1, 2, ..., j_0, \tau_k > 0 \right\}.$$

The calculation grid on spatial variables  $\omega_h$  has the following form:

$$\begin{split} & \omega_{h} = \left\{ 0 \leq x_{1,i_{1}} \leq l_{1}, \ 0 \leq x_{2}, i_{2} \leq l_{2}, \ x_{1,0} = x_{2,0} = 0, \\ & x_{1,i_{1}} = x_{1,0} + i_{1}h_{1}, i_{1} = \overline{l,N_{1}}, \ x_{2,i_{2}} = x_{2,0} + i_{2}h_{2}, i_{2} = \overline{l,N_{2}} \right\}. \end{split}$$

For the effective solution of the Equation (1) we used a locally-one-dimensional method [11]. Let us put a chain of the one-dimensional equations in correspondence with the Eq. (1):

$$\frac{\partial \mathbf{C}_{(1)}^{\mathrm{T}}}{\partial t} = \frac{\partial}{\partial \mathbf{x}_{1}} \left( \mathbf{D}(\boldsymbol{\chi}_{(1)}) \left( \frac{\partial (\tilde{\mathbf{C}} \mathbf{C}_{(1)})}{\partial \mathbf{x}_{1}} + \frac{\tilde{\mathbf{C}} \mathbf{C}_{(1)}}{\boldsymbol{\chi}_{(1)}} \frac{\partial \boldsymbol{\chi}_{(1)}}{\partial \mathbf{x}_{1}} \right) \right), \tag{7}$$
$$\mathbf{t}_{i=1} \le \mathbf{t} \le \mathbf{t}_{i}, \quad (\mathbf{x}_{1}, \mathbf{x}_{2}) \in \mathbf{G},$$

$$\frac{\partial C_{(2)}^{T}}{\partial t} = \frac{\partial}{\partial x_{2}} \left( D(\chi_{(2)}) \left( \frac{\partial (\tilde{C}C_{(2)})}{\partial x_{2}} + \frac{\tilde{C}C_{(2)}}{\chi_{(2)}} \frac{\partial \chi_{(2)}}{\partial x_{2}} \right) \right), \quad (8)$$

 $\mathbf{t}_{j-1} \leq \mathbf{t} \leq \mathbf{t}_j, \quad (\mathbf{x}_1, \mathbf{x}_2) \in \mathbf{G}.$ 

The equations (7) and (8) are connected by the conditions

$$\begin{split} C_{(1)} \Big|_{t=t_{j-1}} &= C_{(2)} \Big|_{t=t_{j-1}}, j = 2, 3, ..., j_0, \\ C_{(2)} \Big|_{t=t_{j-1}} &= C_{(1)} \Big|_{t=t_j}, j = 1, 2, ..., j_0, C_{(1)}^T \Big|_{t=0} &= C_0(x_1, x_2). \end{split}$$

The values of  $\chi_{(1)}$  and  $\chi_{(2)}$  are defined from (3);  $C_{(m)}^{T} = C_{(m)} + \tilde{K}\chi_{(m)}^{4}C_{(m)}^{2}$ , where  $\tilde{K} = K\tilde{C}_{D}$ .

Boundary conditions for the Equations (7) and (8) are the following:

$$D(\chi_{(1)}) \left( \frac{\partial (\tilde{C}C_{(1)})}{\partial x_1} + \frac{\tilde{C}C_{(1)}}{\chi_{(1)}} \frac{\partial \chi_{(1)}}{\partial x_1} \right) = 0, \qquad (9)$$

$$D(\chi_{(2)}) \left( \frac{\partial (\tilde{C}C_{(2)})}{\partial x_{2}} + \frac{\tilde{C}C_{(2)}}{\chi_{(2)}} \frac{\partial \chi_{(2)}}{\partial x_{2}} \right) = 0,$$
(10)  
$$t_{j-1} \le t \le t_{j}, (x_{1}, x_{2}) \in A_{v}, v = 2, 4.$$

One-dimensional problems (7), (9) and (8), (10) are solved along the lines  $x_2 = x_{2,i_2}$ ,  $i_2 = 0, 1, ..., N_2$  and the lines  $x_1 = x_{1,i_1}$ ,  $i_1 = 0, 1, ..., N_1$ , respectively.

According to the theory of a locally-one-dimensional method [11], we assume that the functions  $C_{(2)}$  and  $C_{(2)}^{T}$  are the approximate solution of the problem (1)–(6) at the time moment  $t = t_j$ ,  $j = 1, 2, ..., j_0$ .

The symbols introduced here for difference relations are the same as in [11].

Using the integrointerpolation method [11], we will construct the nonlinear difference Crank-Nicolson schemes for the differential conditions (7)–(10).

For Eq. (7) on the grid  $\omega$  at  $i_2 = 0, 1, 2, ..., N_2$  we have the following difference equations:

$$\begin{split} \left( y_{(1)}^{T}(z_{(1)},y_{(1)}) \right)_{\overline{i}} \Big|_{i_{1}}^{j} &= \frac{1}{2} \Big( \Big( a_{1}(z_{(1)}) \overline{y}_{(1)\overline{x}_{1}} + \overline{a}_{1}(z_{(1)},\overline{y}_{(1)}) z_{(1)\overline{x}_{1}} \Big)_{x_{1}} \Big) \Big|_{i_{1}}^{j} + \\ &+ \frac{1}{2} \Big( \Big( a_{1}(z_{(1)}) \overline{y}_{(1)\overline{x}_{1}} + \overline{a}_{1}(z_{(1)},\overline{y}_{(1)}) z_{(1)\overline{x}_{1}} \Big)_{x_{1}} \Big) \Big|_{i_{1}}^{j-1}, \qquad (11) \\ &i_{1} = 1, \dots, N_{1} - 1, \quad j = 1, 2, \dots, j_{0}, \\ & \text{where } \overline{y}_{(1)} \Big|_{i_{1}, i_{2}} &= \Big( \widetilde{y} \ y_{(1)} \Big) \Big|_{i_{1}, i_{2}}, \quad i_{1} = 0, 1, \dots, N_{1}. \end{split}$$

Using the differential equation (7), on the boundary  $A_1$  we approximate the condition (9) by the following relation:

$$\begin{split} &0,5\,h_1\Big(y_{(1)}^T(z_{(1)},y_{(1)})\Big)_{\overline{t}}\,\Big|_{i_1=0}^j=\frac{1}{2}(a_1(z_{(1)})\overline{y}_{(1)\overline{x}_1}\,+\,\\ &+\overline{a}_1(z_{(1)},\overline{y}_{(1)})z_{(1)\overline{x}_1}\,\Big|_{i_1=1}^j+\frac{1}{2}(a_1(z_{(1)})\overline{y}_{(1)\overline{x}_1}\,+\,\\ &+\overline{a}_1(z_{(1)},\overline{y}_{(1)})z_{(1)\overline{x}_1}\,\Big|_{i_1=1}^{j-1}\,,\quad j=1,2,...,j_0. \end{split}$$

Similarly, on the boundary  $x_1 = l_{x_1}$  relation

$$-0.5h_{1}(y_{(1)}^{T}(z_{(1)}, y_{(1)}))_{\overline{t}}\Big|_{i_{1}=N_{1}}^{j} = \frac{1}{2}(a_{1}(z_{(1)})\overline{y}_{(1)\overline{x}_{1}} + +\overline{a}_{1}(z_{(1)}, \overline{y}_{(1)})z_{(1)\overline{x}_{1}})\Big|_{i_{1}=N_{1}}^{j} + \frac{1}{2}(a_{1}(z_{(1)})\overline{y}_{(1)\overline{x}_{1}} + +\overline{a}_{1}(z_{(1)}, \overline{y}_{(1)})z_{(1)\overline{x}_{1}})\Big|_{i_{1}=N_{1}}^{j-1}, \quad j = 1, 2, ..., j_{0}$$

is obtained.

In Eq. (11)–(13) the grid functions  $a_1(z_{(1)})$  and  $\overline{a}_1(z_{(1)}, \overline{y}_{(1)})$  are defined as follows:

$$\begin{split} &a_{1}\left(z_{(1)}\right) = 0,5 \left(D\left(z_{(1)}\left(x_{i_{1}}, x_{i_{2}}, t_{j}\right)\right) + D\left(z_{(1)}\left(x_{i_{1}-1}, x_{i_{2}}, t_{j}\right)\right)\right),\\ &\overline{a}_{1}\left(z_{(1)}, \overline{y}_{(1)}\right) = 0,5 \left(D\left(z_{(1)}\left(x_{i_{1}}, x_{i_{2}}, t_{j}\right)\right) \frac{\overline{y}_{(1)}\left(x_{i_{1}}, x_{i_{2}}, t_{j}\right)}{z_{(1)}\left(x_{i_{1}}, x_{i_{2}}, t_{j}\right)} + \\ &+ D\left(z_{(1)}\left(x_{i_{1}-1}, x_{i_{2}}, t_{j}\right)\right) \frac{\overline{y}_{(1)}\left(x_{i_{1}-1}, x_{i_{2}}, t_{j}\right)}{z_{(1)}\left(x_{i_{1}-1}, x_{i_{2}}, t_{j}\right)}\right),\\ &i_{1} = 1, 2, \dots, N_{1}, \quad i_{2} = 0, 1, \dots, N_{2}, \quad j = 0, 1, \dots, j_{0}. \end{split}$$

Similarly, the differential equation (8) on the grid  $\omega$ at  $i_1 = 0, 1, ..., N_1$  is approximated by the difference relations of the form

$$\begin{split} \left(\mathbf{y}_{(2)}^{\mathrm{T}}(\mathbf{z}_{(2)},\mathbf{y}_{(2)})\right)_{\overline{t}}\Big|_{i_{2}}^{j} &= \\ &= \frac{1}{2} \Big( \Big( a_{2}(\mathbf{z}_{(2)})\overline{\mathbf{y}}_{(2)\overline{\mathbf{x}}_{2}} + \overline{a}_{2}(\mathbf{z}_{(2)},\overline{\mathbf{y}}_{(2)}) \mathbf{z}_{(2)\overline{\mathbf{x}}_{2}} \Big)_{\mathbf{x}_{2}} \Big) \Big|_{i_{1}}^{j} + \\ &+ \frac{1}{2} \Big( \Big( a_{2}(\mathbf{z}_{(2)})\overline{\mathbf{y}}_{(2)\overline{\mathbf{x}}_{2}} + \overline{a}_{2}(\mathbf{z}_{(2)},\overline{\mathbf{y}}_{(2)}) \mathbf{z}_{(2)\overline{\mathbf{x}}_{2}} \Big)_{\mathbf{x}_{2}} \Big) \Big|_{i_{2}}^{j-1}, \\ &\mathbf{i}_{2} = 1, \dots, \mathbf{N}_{2} - 1, \quad \mathbf{j} = 1, 2, \dots, \mathbf{j}_{0}. \\ &\quad \text{Here } \left. \overline{\mathbf{y}}_{(2)} \right|_{i_{1}, i_{2}} = \Big( \widetilde{\mathbf{y}} \mathbf{y}_{(2)} \Big) \Big|_{i_{1}, i_{2}}, \quad \mathbf{i}_{2} = 0, 1, \dots, \mathbf{N}_{2}. \end{split}$$
(14)

For the boundary condition (10) on the boundary line  $A_2$  we construct the difference approximation

$$\begin{split} &0.5 h_2 \Big( y_{(2)}^{\mathsf{T}}(z_{(2)}, y_{(2)}) \Big)_{\overline{t}} \Big|_{i_2=0}^j = \frac{1}{2} \big( a_2(z_{(2)}) \overline{y}_{(2)\overline{x}_2} + \\ &+ \overline{a}_2(z_{(2)}, \overline{y}_{(2)}) z_{(2)\overline{x}_2} \big) \Big|_{i_2=1}^j + \frac{1}{2} \big( a_2(z_{(2)}) \overline{y}_{(2)\overline{x}_2} + \\ &+ \overline{a}_2(z_{(2)}, \overline{y}_{(2)}) z_{(2)\overline{x}_2} \big) \Big|_{i_2=1}^{j-1}, \quad j = 1, 2, ..., j_0. \end{split}$$
(15)

Similarly, for  $(x_1, x_2) \in A_4$  we obtain the following difference relations

$$-0.5 h_{2} \left( y_{(2)}^{T}(z_{(2)}, y_{(2)}) \right)_{\overline{t}} \Big|_{i_{2}=N_{2}}^{j} = \frac{1}{2} (a_{2}(z_{(2)}) \overline{y}_{(2)\overline{x}_{2}} + + \overline{a}_{2}(z_{(2)}, \overline{y}_{(2)}) z_{(2)\overline{x}_{2}} \Big|_{i_{2}=N_{2}}^{j} + \frac{1}{2} (a_{2}(z_{(2)}) \overline{y}_{(2)\overline{x}_{2}} + (16) + \overline{a}_{2}(z_{(2)}, \overline{y}_{(2)}) z_{(2)\overline{x}_{2}} \Big|_{i_{2}=N_{2}}^{j-1}, \quad j = 1, 2, ..., j_{0}.$$

In the relations (14)–(16) the grid functions  $a_2(z_{(2)})$  and  $\overline{a}_2(z_{(2)}, \overline{y}_{(2)})$  are defined as follows:

$$\begin{split} & a_{2}\left(z_{(2)}\right) = 0, 5\left(D\left(z_{(2)}\left(x_{i_{1}}, x_{i_{2}}, t_{j}\right)\right) + D\left(z_{(2)}\left(x_{i_{1}}, x_{i_{2}-1}, t_{j}\right)\right)\right), \\ & \overline{a}_{2}\left(z_{(2)}, \overline{y}_{(2)}\right) = 0, 5\left(D\left(z_{(2)}\left(x_{i_{1}}, x_{i_{2}}, t_{j}\right)\right) \frac{\overline{y}_{(2)}\left(x_{i_{1}}, x_{i_{2}}, t_{j}\right)}{z_{(2)}\left(x_{i_{1}}, x_{i_{2}}, t_{j}\right)} + , \\ & + D\left(z_{(2)}\left(x_{i_{1}}, x_{i_{2}-1}, t_{j}\right)\right) \frac{\overline{y}_{(2)}\left(x_{i_{1}}, x_{i_{2}-1}, t_{j}\right)}{z_{(2)}\left(x_{i_{1}}, x_{i_{2}-1}, t_{j}\right)}\right) \\ & i_{1} = 0, 1, ..., N_{1}, \quad i_{2} = 1, 2, ..., N_{2}, \quad j = 0, 1, ..., j_{0}. \end{split}$$

Problems (11)–(13) and (14)–(16) are connected by the following conditions

$$|\mathbf{y}_{(1)}|_{t=t_{j-1}} = |\mathbf{y}_{(2)}|_{t=t_{j-1}}, |\mathbf{y}_{(2)}|_{t=t_{j-1}} = |\mathbf{y}_{(1)}|_{t=t_{j}}, |\mathbf{y}_{(1)}^{T}|_{t=0} = C_{0}(\mathbf{x}_{1}, \mathbf{x}_{2}).$$

We complete the system of the difference relations (11)-(13), (14)-(16) and (17) by algebraic nonlinear equations

$$z_{(m)} - \frac{1}{2n_{e}} \left( y_{(m)} - \tilde{K} z_{(m)}^{4} y_{(m)}^{2} - C_{B} + \sqrt{\left( y_{(m)} - \tilde{K} z_{(m)}^{4} y_{(m)}^{2} - C_{B} \right)^{2} + 4n_{e}^{2}} \right) \Big|_{i_{1}, i_{2}}^{j} = 0,$$
(17)
where

 $m=1,2; \quad j=0,1,...,j_0; \quad i_1=0,1,...,N_1; \quad i_2=0,1,...,N_2.$ 

We construct the initial conditions for the difference problem (11)–(13) using the relations (3) and (5):

$$\begin{aligned} \left| y_{(1)} + \tilde{K} z_{(1)}^{4} y_{(1)}^{2} &= C_{0} \right|_{i_{1},i_{2}}, \\ z_{(1)} - \frac{1}{2n_{e}} \left( y_{(1)} - \tilde{K} z_{(1)}^{4} y_{(1)}^{2} - C_{B} + \sqrt{\left( y_{(1)} - \tilde{K} z_{(1)}^{4} y_{(1)}^{2} - C_{B} \right)^{2} + 4n_{e}^{2}} \right) \right|_{i_{1},i_{2}} &= 0, \\ \text{where } i_{1} = 0, 1, ..., N_{1}, i_{2} = 0, 1, ..., N_{2}, \end{aligned}$$

$$(18)$$

where  $l_1 = 0, l, ..., N_1, l_2 = 0, l, ..., N_2$ 

Approximate solution of the algebraic equations system (18) is obtained by the method of interval bisection.

On the grid  $\omega_h$  the equation (2) is approximated by the following system of the difference relations:

$$\left(\sum_{k=1}^{2} \tilde{y}_{\bar{x}_{k}x_{k}} - \frac{\tilde{y}}{l_{i}^{\times 2}} + \frac{\tilde{C}^{g}}{l_{i}^{\times 2}}\right)\Big|_{i_{1},i_{2}} = 0,$$
(19)

 $i_1 = 1, 2, ..., N_1 - 1; \quad i_2 = 1, 2, ..., N_2 - 1.$ 

The difference equations (19) jointly with the corresponding boundary conditions are solved by the block-Thomas algorithm [14].

The difference relations (11)–(19) are the closed system of the nonlinear algebraic equations for every  $j = 1, 2, ..., j_0$ . We find the solution of this system using the same iterative processes.

For the nonlinear equation (11) at  $i_2 = 0, 1, ..., N_2$  we construct the following iterative process

$$\begin{split} & \left(y_{(1)}^{T}\left(z_{(1)}^{s}y_{(1)}^{s}\right) + \left(1 + 2\gamma_{(1)}^{s}y_{(1)}^{s}\right)\left(z_{(1)}^{s+1} - z_{(1)}^{s}\right)\right)\right|_{i_{1}}^{j} = y_{(1)}^{T}\left(z_{(1)}y_{(1)}\right)\right|_{i_{1}}^{j-1} + \\ & + \frac{\tau_{j}}{2}\left(\left(a_{1}(z_{(1)}^{s})\tilde{y}y_{(1)\overline{x}_{1}}^{s+1} + \overline{a}_{(1)}(z_{(1)}^{s}, y_{(1)}^{s})z_{(1)\overline{x}_{1}}^{s}\right)_{x_{1}}\right)\right|_{i_{1}}^{j} + \\ & + \frac{\tau_{j}}{2}\left(\left(a_{1}(z_{(1)})\overline{y}_{(1)\overline{x}_{1}} + \overline{a}_{(1)}(z_{(1)}, y_{(1)})z_{(1)\overline{x}_{1}}\right)_{x_{1}}\right)\right|_{i_{1}}^{j-1}. \end{split}$$

Here  $\stackrel{s}{\gamma}_{(1)} = K \stackrel{s^4}{z}_{(1)}, \quad \stackrel{s}{\overline{y}}_{(1)} = \tilde{y} \stackrel{s}{y}_{(1)};$  $i_1 = 1, 2, ..., N_1 - 1; \quad s = 0, 1, 2, ....$ 

For the boundary conditions (12) and (13) we have, respectively

$$\begin{split} \xi_{j} \Bigg( y_{(1)}^{T} \Bigg( z_{(1)}^{s} y_{(1)}^{s} \Bigg) + \Bigg( 1 + 2\gamma_{(1)}^{s} y_{(1)}^{s} \Bigg) \Bigg( z_{(1)}^{s+1} - z_{(1)}^{s} y_{(1)}^{s} \Bigg) \Bigg) \bigg|_{i_{1}=0}^{j} = \\ &= \xi_{j} \ y_{(1)}^{T} \Bigg( z_{(1)} y_{(1)} \Bigg) \bigg|_{i_{1}=0}^{j-1} + \frac{1}{2} \Bigg( a_{1} (z_{(1)}) \tilde{y} y_{1(1)\overline{x}_{1}}^{s+1} + \overline{a}_{1} (z_{(1)}, \overline{y}_{(1)}) z_{(1)\overline{x}_{1}} \Bigg) \bigg|_{i_{1}=1}^{j} + \\ &+ \frac{1}{2} \Bigg( a_{1} (z_{(1)}) \overline{y}_{(1)\overline{x}_{1}} + \overline{a}_{1} (z_{(1)}, \overline{y}_{(1)}) z_{(1)\overline{x}_{1}} \Bigg) \bigg|_{i_{1}=1}^{j-1} ; \qquad (21) \\ &- \\ &\xi_{j} \Bigg( y_{(1)}^{T} \Bigg( z_{(1)}^{s} y_{(1)} \Bigg) + \Bigg( 1 + 2\gamma_{(1)}^{s} y_{(1)} \Bigg) \Bigg( z_{(1)}^{s+1} - z_{(1)}^{s} y_{(1)} \Bigg) \bigg) \bigg|_{i_{1}=N_{1}}^{j} = \\ &= (z_{1} - z_{1}) \bigg( z_{1} - z_{1} - z_{1}) \bigg) \bigg|_{i_{1}=N_{1}}^{j} = \\ &z_{1} - z_{1} - z_{1} - z_{1} \bigg( z_{1} - z_{1} - z_{1} \bigg) \bigg( z_{1} - z_{1} - z_{1} \bigg) \bigg) \bigg|_{i_{1}=N_{1}}^{j} = \\ &z_{1} - z_{1} - z_{1} - z_{1} \bigg( z_{1} - z_{1} - z_{1} \bigg) \bigg( z_{1} - z_{1}$$

$$= -\xi_{j} \mathbf{y}_{(1)}^{\mathrm{T}} \left( z_{(1)} \mathbf{y}_{(1)} \right) \Big|_{i_{1}=N_{1}}^{s} + + \frac{1}{2} \left( a_{1} \left( z_{(1)}^{s} \right) \tilde{\mathbf{y}} \mathbf{y}_{(1)\overline{x}_{1}}^{s+1} + \overline{a}_{1} \left( z_{(1)}^{s} , \overline{\mathbf{y}}_{(1)}^{s} \right) z_{(1)\overline{x}_{1}}^{s} \right)_{i_{1}=N_{1}}^{s} + \\ + \frac{1}{2} \left( a_{1} (z_{(1)}) \overline{\mathbf{y}}_{(1)\overline{x}_{1}} + \overline{a}_{1} (z_{(1)}, \overline{\mathbf{y}}_{(1)}^{s} ) z_{(1)\overline{x}_{1}}^{s} \right)_{i_{1}=N_{1}}^{j-1},$$
(22)

where  $\xi_j = 0.5h_1 / \tau_j$ , s = 0, 1, 2, ....

The solution of the problem (20)–(22) is obtained by the Thomas algorithm [11]. By analogy with the relations (20)–(22) we construct the iterative procedures for the solution of the nonlinear equations (14)–(16). For the equation (17) we obtain the following iterative relation  $\int_{Z(m)}^{s+1} \frac{1}{2} \times dx$ 

$$\begin{pmatrix} s_{1} \\ y_{(m)} - K \\ z_{(m)} & y_{(m)} - C_{B} \\ + \sqrt{\begin{pmatrix} s_{1} \\ y_{(m)} - K \\ z_{(m)} & y_{(m)} - C_{B} \end{pmatrix}^{2} + 4n_{e}^{2}} \\ m = 1, 2, \quad j = 0, 1, ..., j_{0}, \quad i_{1} = 0, 1, ..., N_{1}, \quad i_{2} = 0, 1, ..., N_{2}, \quad s = 0, 1, 2, ...$$

The values of the grid functions  $z_{(m)}^{s+1}$ , m = 1, 2, s = 0, 1, 2, ..., on the grid  $\omega$  taking into account  $y_{(m)}^{s+1}$  is calculated by the method of interval bisection.

The iterations are stopped when

$$\begin{split} & \left| \begin{matrix} s^{s+1} \\ y^{(1)i_1,i_2} - \begin{matrix} s \\ y^{(1)i_1,i_2} \end{matrix} \right| \leq \epsilon \left| \begin{matrix} s \\ y^{(1)i_1,i_2} \end{matrix} \right|, \quad i_1 = 0, 1, ..., N_1, \\ & i_2 = 0, 1, ..., N_2, \quad s = 1, 2, ..., \end{split}$$

where  $\varepsilon$  is empirical parameter.

We assume that the numerical solution  $y_{(2)}$  is an approximate solution of the problem (1)–(6) at every time layer.

Control of the calculations is realized by the testing of the condition

$$\begin{split} \iint_{G} y_{(2)}^{T}(x_{1}, x_{2}, t^{j}) dx_{1} dx_{2} &= \iint_{G} C_{0}(x_{1}, x_{2}) dx_{1} dx_{2} ,\\ j &= 1, 2, ..., j_{0} , \end{split}$$
 where  $y_{(2)}^{T} &= y_{(2)} + K z_{(2)}^{4} y_{(2)}^{2} . \end{split}$ 

# **III. Results of simulation**

We simulated the experiment described in [5]:  $10^{15}$  cm<sup>-2</sup> 15 keV As<sup>+</sup> ions were implanted at room temperature into Si wafers with (100) orientation and ptype resistivity of 2.5–5.2  $\Omega$ ·cm. After the ion implantation, the wafers were annealed in a tungstenhalogen lamp system in nitrogen ambient at a temperature of 950 °C for 10 s. The arsenic concentration profile after annealing was measured by ToF-SIMS. The concentration scale for As has been determined using known calibration standard implantations in Si (absolute error 10%), and the depth scale has been determined using ex situ interference microscopy (absolute error < 5%), assuming a constant erosion rate [5].

For the calculation of point defects distribution we used the following values:  $a = 0.5 \,\mu\text{m}$ ,  $\alpha = 0.175$ ,  $\beta = 0$ ,  $l_i^x = 0.05 \,\mu\text{m}$ ,  $l_1 = 0.4 \,\mu\text{m}$ ,  $l_2 = 5 \,\mu\text{m}$ . In Fig. 1, the calculated values of the point defects distribution  $\tilde{C}$  are presented.

For the simulation of As diffusion we used the following parameters:  $l_1 = 0,2 \text{ µm}$ ,  $l_2 = 1 \text{ µm}$ ,  $\beta_1 = 0,436$ ;  $\beta_2 = 0,0$ ;  $\tilde{K} = 3,0 \times 10^{-16} \text{ µm}^3$ . In Fig. 2, the two-dimensional profile of As distribution  $C^T$  as a result of rapid thermal annealing is presented. In Fig. 3, results of simulation at  $x_2 = 0$  are compared with the experimental data [5].

The calculated profile of the total As concentration agrees well with the experimental data, including the near surface region (Figs. 2, 3). Therefore, the presented model allows simulation of high concentration transient enhanced diffusion of As implanted in Si. The transport process differs substantially from the processes described by the Fick's second law. In our opinion, the non-uniform distribution of point defects plays the main role in the "uphill" diffusion of arsenic atoms near the surface of the semiconductor and formation of local maximum of the dopant concentration. It follows from Eq. (1) that nonuniform distribution of silicon interstitial atoms in the neutral charge state causes the additional flux of impurity atoms, which leads to the "uphill" diffusion. We suppose that radiation induced segregation or matrix effects during SIMS analysis are negligible, because apparent "uphill" diffusion is not observed for the as-implanted As profiles also measured by SIMS.



Fig. 2. Simulated two-dimensional As distribution after annealing.



**Fig. 3.** Simulated As profile before (1) and after annealing (3) compared to experimental profile (2) from [5].

# Conclusion

The two-dimensional model of thermal diffusion of arsenic in silicon was developed. We applied the effective difference method of the solving of the constructed system of the differential equations. The offered nonlinear model considers interaction of high concentration of impurity, point defects and electrons. The model can be used for in modern integrated circuits manufacturing technology for the simulation of rapid thermal annealing. The model predicts the effect of "uphill" diffusion of the implanted arsenic in surface areas of silicon crystal. The simulation results are in a reasonable agreement with experimental data, including the presence of local maximum of the arsenic atoms near the surface.

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# Моделювання швидкого теплового відпалу низько-енергетичної імплантації миш'яку у кремній

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Представлена двомірна модель теплової дифузії. Дана модель була запропонована з врахуванням нелінійності процесу, формування кластерів та впливу точкових дефектів. Для розрахунку профілю домішкового розподілу за швидкого термічного відпалу був використаний ефективний числовий алгоритм оснований на методі кінцевої різниці. Результати теоретичних розрахунків близькі до експериментальних даних.